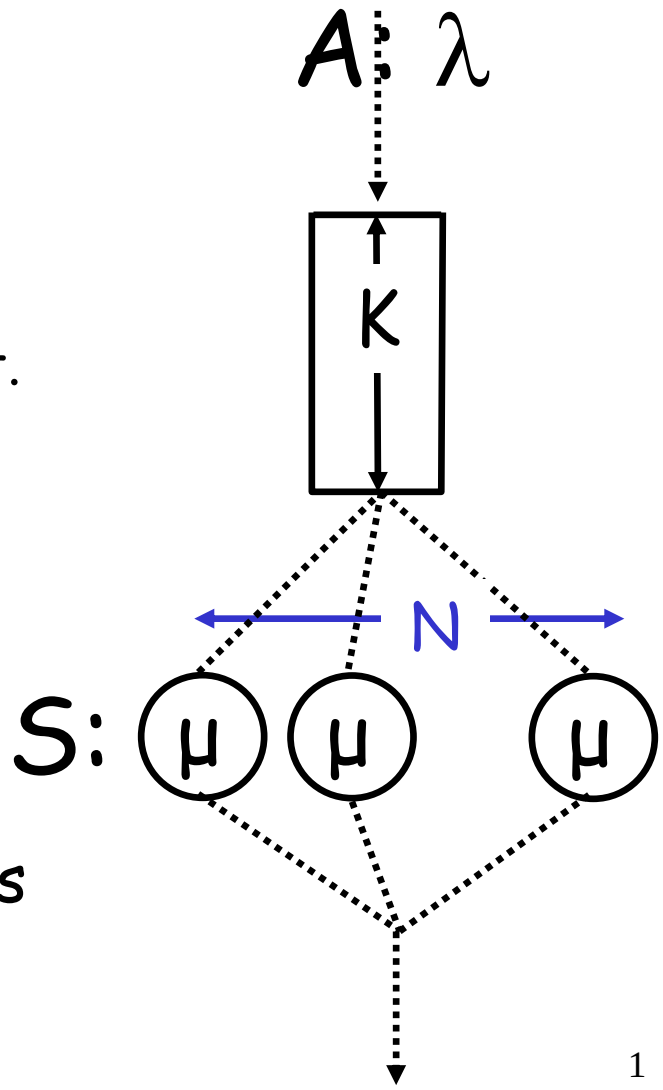
A/S/N/K systems (Kendall's notation)

A/S/N/K gives a theoretical description of a system

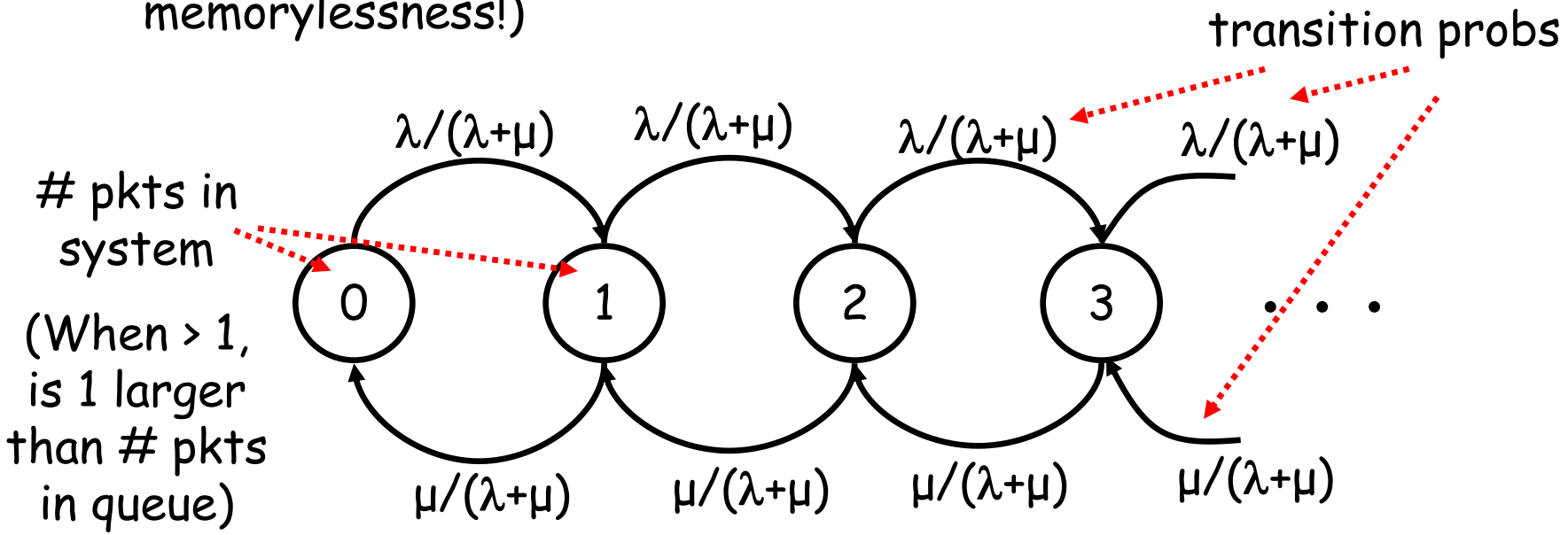
- A is the arrival process
  - M = Markovian = Poisson Arrivals
  - D = deterministic (constant time bet. arrivals)
  - G = general (anything else)
- S is the service process
  - M,D,G same as above
- N is the number of parallel processors
- K is the buffer size of the queues
  - K term can be dropped when buffer size is infinite



The M/M/1 Queue (a.k.a., birth-death process)

- a.k.a., M/M/1/∞
  - Poisson arrivals
  - Exponential service time
  - 1 processor, infinite length queue
- Can be modeled as a Markov Chain (because of memorylessness!)

- Distribution of time spent in state n the same for all n > 0 (why? why different for state 0?)



M/M/1 cont'd

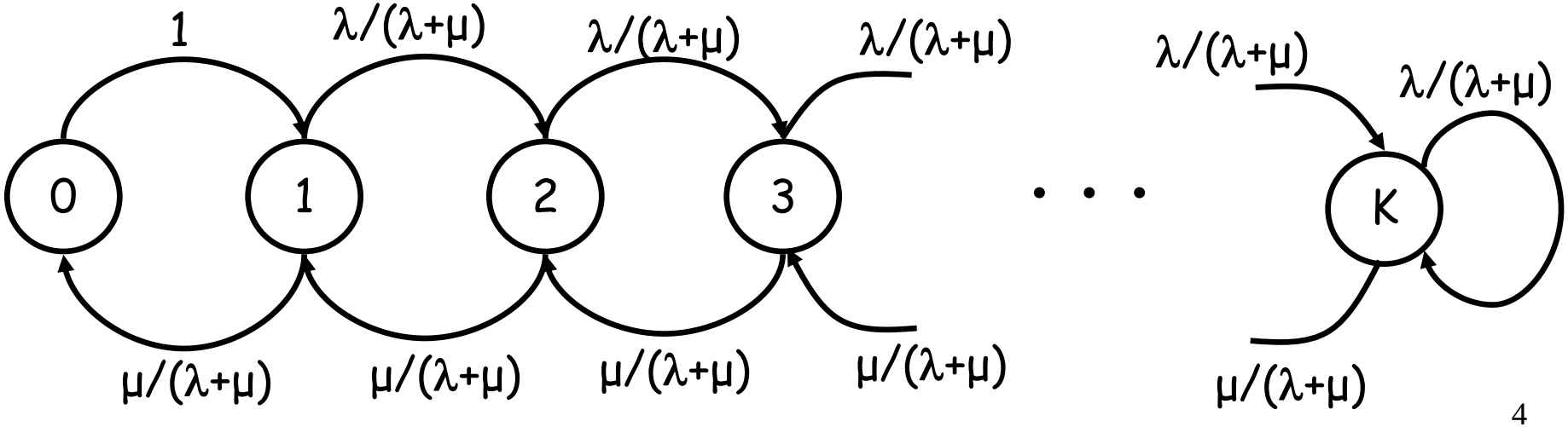
As long as $\lambda < \mu$, queue has following steady-state average properties

- Defs:
  - $\rho = \lambda/\mu$
  - N = # pkts in system
  - T = packet time in system
  - N_Q = # pkts in queue
  - W = waiting time in queue

- $P(N=n) = \rho^n(1-\rho)$
  - (indicates fraction of time spent w/ n pkts in queue)
  - Utilization factor = $1 - P(N=0) = \rho$
- $E[N] \equiv \sum_{n=0}^{\infty} n\, P(N=n) = \rho/(1-\rho)$
- $E[T] = E[N] / \lambda$ (Little's Law) $= \rho/(\lambda(1-\rho)) = 1 / (\mu - \lambda)$
- $E[N_Q] = \sum_{n=1}^{\infty} (n-1)\, P(N=n) = \rho^2/(1-\rho)$
- $E[W] = E[T] - 1/\mu$ (or $= E[N_Q]/\lambda$ by Little's Law) $= \rho / (\mu - \lambda)$

M/M/1/K queue

- Also can be modeled as a Markov Model
  - requires K+1 states for a system (queue + processor) that holds K packets (why?)
  - Stay in state K upon a packet arrival
  - Note: $\rho \geq 1$ permitted (why?)



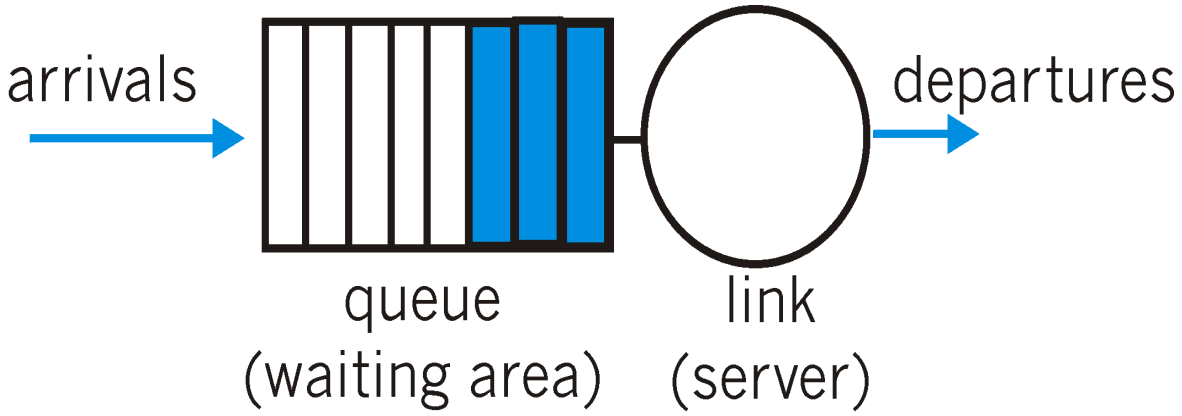
M/M/1/K properties

- $P(N=n) = \begin{cases} \rho^n(1-\rho) / (1 - \rho^{K+1}), & \rho \neq 1 \\ 1 / (K+1), & \rho = 1 \end{cases}$
- $E[N] = \begin{cases} \rho/((1-\rho)(1 - \rho^{K+1})), & \rho \neq 1 \\ 1 / (K+1), & \rho = 1 \end{cases}$
- i.e., divide M/M/1 values by $(1 - \rho^{K+1})$

Scheduling And Policing Mechanisms

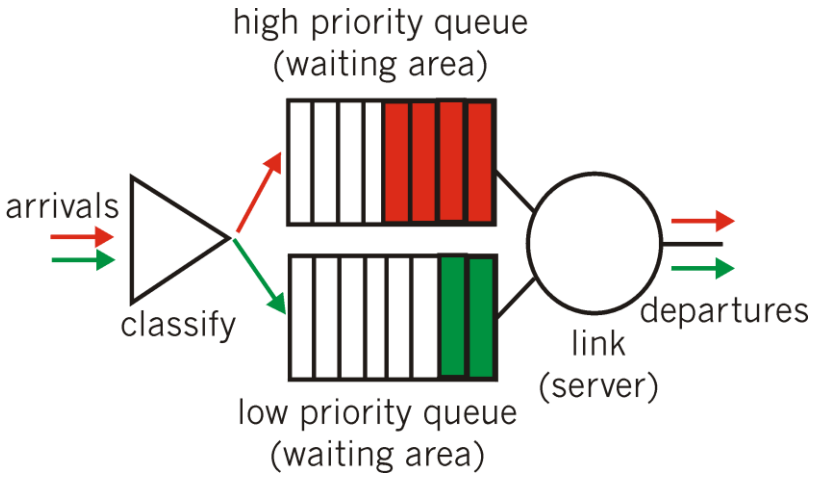
Scheduling: choosing the next packet for transmission on a link can be done following a number of policies;

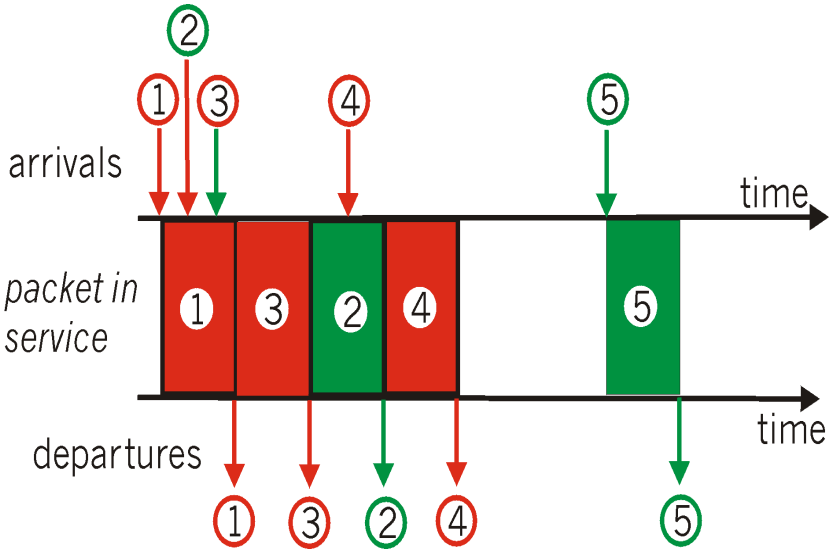
- FIFO (First In First Out) a.k.a. FCFS (First Come First Serve): in order of arrival to the queue
  - packets that arrive to a full buffer are discarded
  - another option: discard policy determines which packet to discard (new arrival or something already queued)



Scheduling Policies

- Priority Queuing:
  - Classes have different priorities
  - May depend on explicit marking or other header info, eg IP source or destination, TCP Port numbers, etc.
  - Transmit a packet from the highest priority class with a non-empty queue

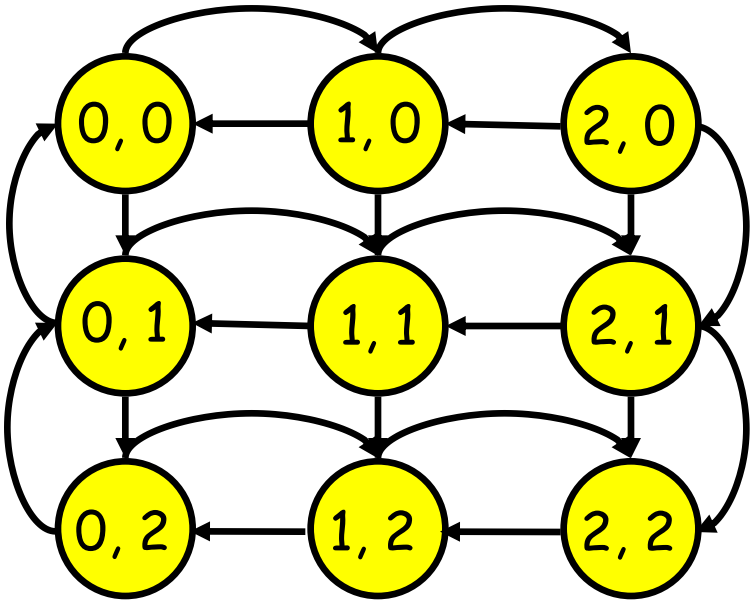




Scheduling Policies

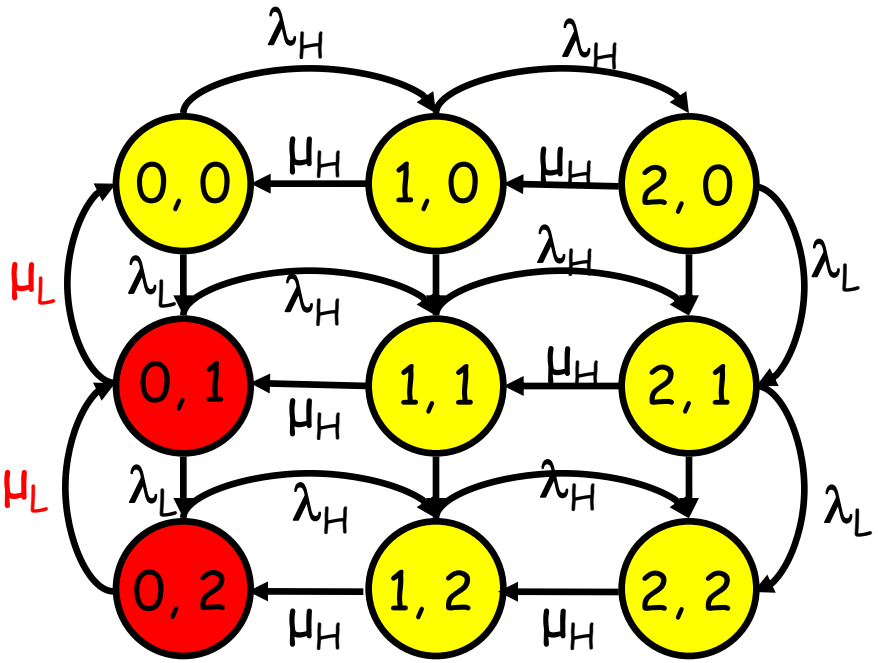
- Priority Queueing cont'd:
  - 2 versions:
    - Preemptive: (postpone low-priority processing if high-priority pkt arrives)
    - non-preemptive: any packet that starts getting processed finishes before moving on

Modeling priority queues as M/M/1/K



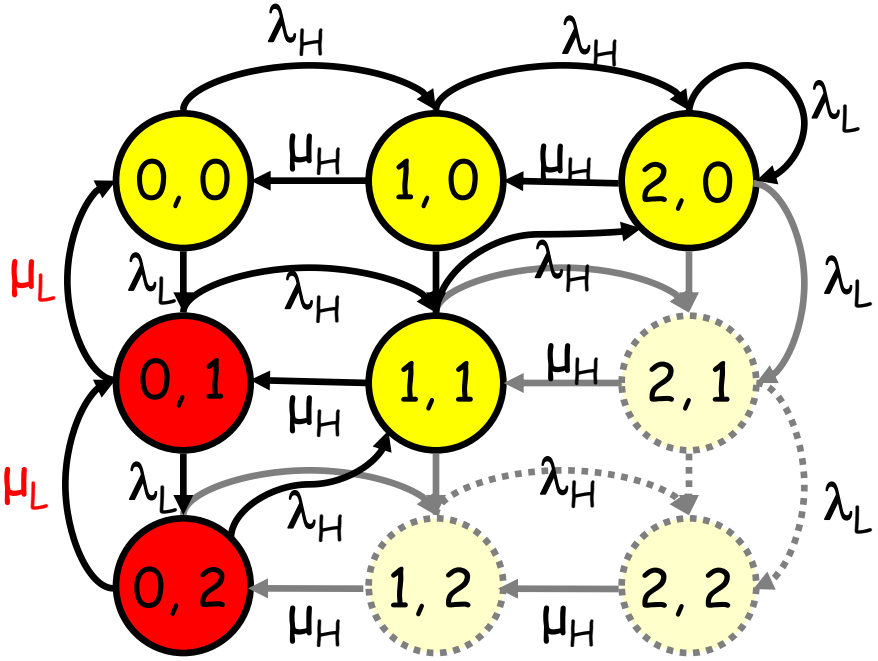
- preemptive version (K=2): assuming preempted packet placed back into queue
  - state w/ x,y indicates x priority queued, y non-priority queued
  - what are the transition probabilities?
  - what if preempted is discarded?

Modeling priority queues as M/M/1/K



- preemptive version (K=2 for each priority)
  - state w/ x,y indicates x priority queued, y non-priority queued

M/M/1/K Priority Queue: Pre-empted Job Discarded



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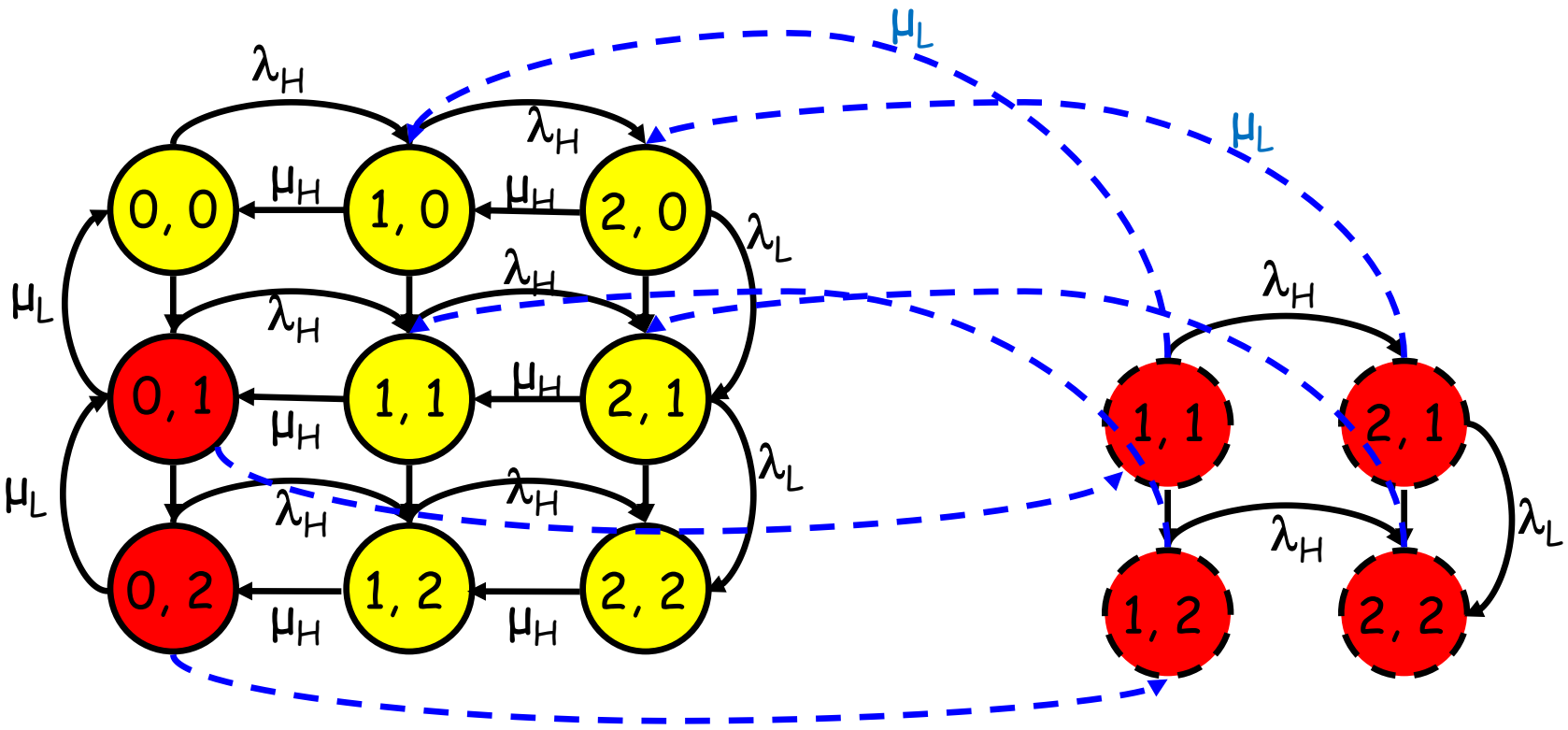
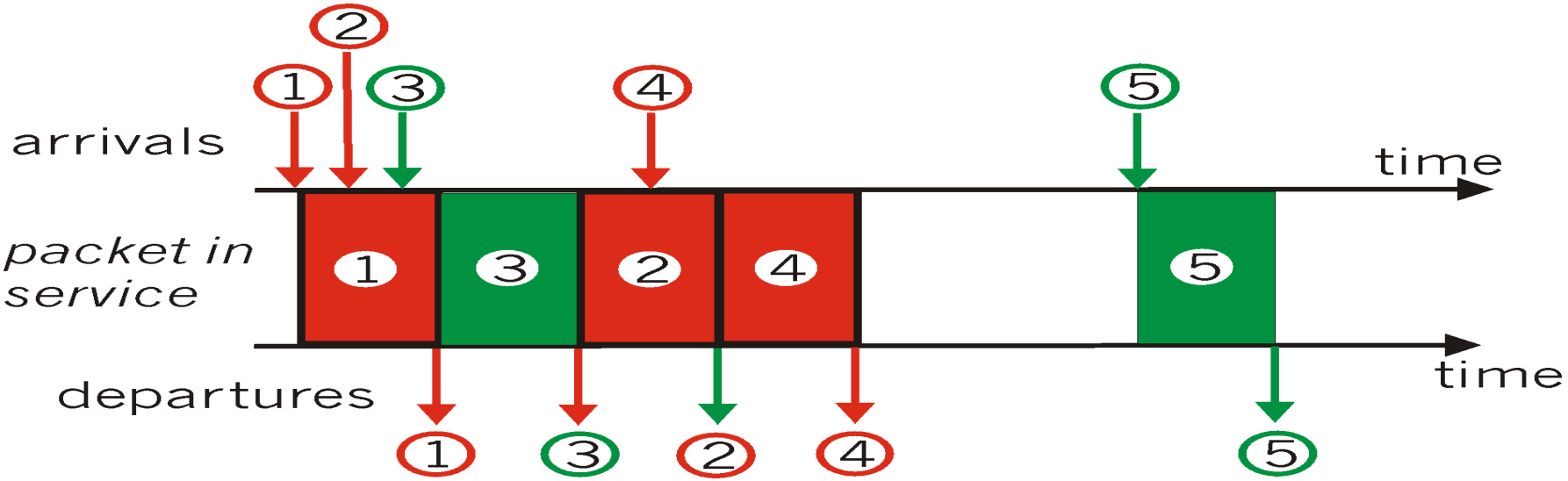
Modeling priority queues as M/M/1/K



- Non-preemptive version (K=2)
  - yellow (solid border) = nothing or high-priority being proc'd
  - red (solidborder) = low-priority being processed
  - red (dashed border) = nothing/high-priority being processed
  - what are the transition probabilities?

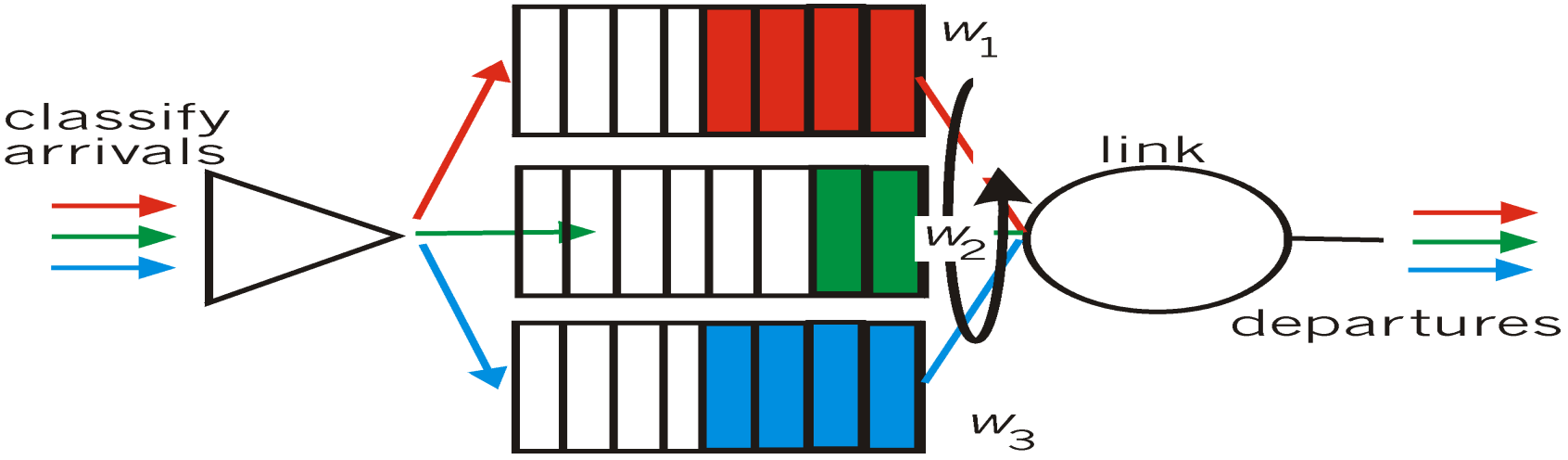
Scheduling Policies (more)

- Round Robin:
  - each flow gets its own queue
  - circulate through queues, process one pkt (if queue non-empty), then move to next queue



Scheduling Policies (more)

- Weighted Fair Queuing: is a generalized Round Robin in which an attempt is made to provide a class with a differentiated amount of service over a given period of time



WFQ details

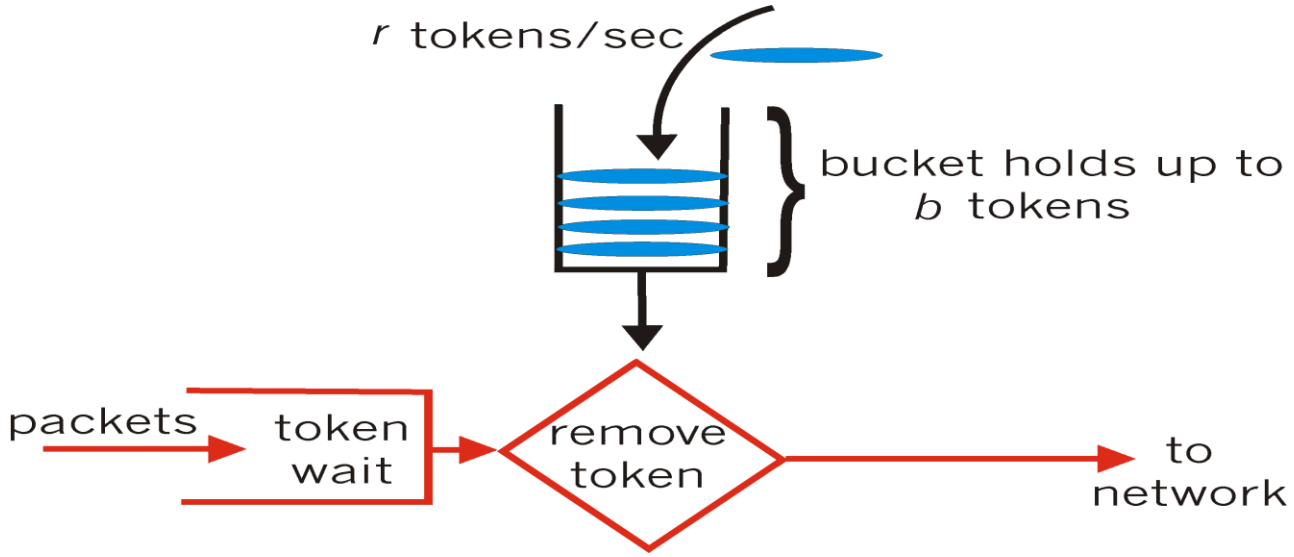
- Each flow, i, has a weight, $W_i > 0$
- A Virtual Clock is maintained: V(t) is the "clock" at time t
- Each packet k in each flow i has
  - virtual start-time: $S_{i,k}$
  - virtual finish-time: $F_{i,k}$
- The Virtual Clock is restarted each time the queue is empty
- When a pkt arrives at (real) time t, it is assigned:
  - $S_{i,k} = \max\{F_{i,k-1}, V(t)\}$
  - $F_{i,k} = S_{i,k} + \text{length}(k) / W_i$
  - $V(t) = V(t') + (t-t') / \sum_{B(t',t)} W_j$
    - t' = last time virtual clock was updated
    - B(t',t) = set of sessions with pkts in queue during (t',t]

Policing Mechanisms

- Three criteria:
  - (Long term) **Average Rate** (100 packets per sec or 6000 packets per min??), crucial aspect is the interval length
  - **Peak Rate**: e.g., 6000 p p minute Avg and 1500 p p sec Peak
  - (Max.) **Burst Size**: Max. number of packets sent consecutively, ie over a short period of time

Policing Mechanisms

- Token Bucket mechanism, provides a means for limiting input to specified Burst Size and Average Rate.



Policing Mechanisms (more)

- Bucket can hold b tokens; token are generated at a rate of *r token/sec* unless bucket is full of tokens.
- Over an interval of length *t*, the number of packets that are admitted is less than or equal to (*r t + b*).
- Token bucket and WFQ can be combined to provide upper bound on delay.